Quantification of devastating climate events under climate change through novel multivariate bias correction methods

## Séminaire Géolearning

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A combination of multiple drivers and/or hazards that contributes to societal or environmental risk (Zscheischler et al., 2020)



## **PHD Objective**



# Modelling the dependence

• With climate change, or in the simulations, the marginals and the dependence structure can change.

 Multivariate bias correction is probably necessary to affect both the marginals and the dependence.





## Multivariate extreme value theory

 X<sub>N</sub> and Y<sub>N</sub> are two samples with bivariate cumulative distribution function F, supposedly in the domain of attraction of a bivariate extreme value cumulative distribution function G.

- Sklar's theorem (1959) : Any multivariate cumulative distribution function **F** can be expressed in terms of its margins  $F_i$  and a copula **C** :  $F(x_1, ..., x_d) = C(F_1(x_1), ..., F_d(x_d))$  with  $\mathbf{C} : [0,1]^d \rightarrow [0,1]$
- Therefore, we get weak convergence of the marginal distribution functions and the copula function

# **Copulas and uniform margins**

• This allows us to propose the following approach :

- 1. Propose a univariate extreme model for the marginals
- 2. Reduce to uniform margins
- 3. Determine the copula

• X<sub>N</sub> and Y<sub>N</sub> must be i.i.d. and extreme, and (X<sub>N</sub>, Y<sub>N</sub>) must be extreme in some sense

## **Three potential events**

- July 2021 Belgian/German flooding (Preconditioned event)
- May/June 2016 French flooding (Spatially compound event)

- Convective cells
- (Multivariate compound event)



# 14<sup>th</sup> July 2021 flooding

• Data from ERA5 reanalyzes

Total Precipitation (TP) : daily precipitation (mm/day)

• Antecedent Precipitation Index (API) :  $API_j = \sum_{i=1}^{i=N} k^{i-1} * TP_{j-i}$ with k=0.9 and N=30



## **Data Selection**

#### Data must be i.i.d. and extreme

#### Data selection for 1D

- For TP : select points above the 95<sup>th</sup> quantile, separated by at least 2 days
- For API : select points above the 95<sup>th</sup> quantile, separated by at least D days, with :

 $\rho(API_j, API_{j+D}) < 0,1$  (D = 20)

#### Data selection for 2D

- Select  $(TP_i, API_j)$  with  $TP_i > Q95_{TP}, API_j > Q95_{API}$  and  $i 5 \le j \le i$
- Then select couples separated by at least D days, according to the highest TP value

### **Data selection**



## **Generalized Pareto Distribution model**

With the univariate data selection, we can use a Generalized Pareto Distribution (GPD) model :

$$F(x) = 1 - (1 + \xi x)^{\frac{-1}{\xi}}$$

with  $x \ge 0$  and  $\xi \ne 0$ 

Parameters are estimated through maximum likelihood method



#### **Quantile plots of GPD adjustment**

**QQplot TP (ERA)** х 30 25 х 20 χχΧ 15 15 20 25 30 theoretical guantiles = 0,016 (0,060)

empirical quantiles



## **Copula model estimation**

Use maximum likelihood to estimate the parameters of all the copulas from the selection : Gaussian, student, Archimedean

Then select the best copula according to the Akaike Information Criteria (AIC)



### **Coefficients of extremal dependence**

For (U, V) uniform r.v., we define 
$$\chi$$
:  $\chi = \lim_{u \to 1} P(V > u | U > u)$   
and  $P(V > u | U > u) \approx 2 - \frac{\log C(u,u)}{\log u}$ 

Similarly, we can define 
$$\bar{\chi}$$
:  $\bar{\chi} = \lim_{u \to 1} \frac{2\log(1-u)}{\log \bar{C}(u,u)} - 1$   
With  $\bar{C}(u,v) = 1 - u - v + C(u,v)$ 

Here, we have :  $(\chi, \overline{\chi}) = (0, -0.019) --->$  asymptotic independence, close to total independence

## **Return periods**

Univariate return period = inverse of the probability to exceed a determined threshold :

$$T(x_{14.07}) = \frac{1/n}{1 - P(X \le x_{14.07})}$$

 When describing a bivariate event by a joint exceedance (AND), the return period is defined by :

$$T_B(TP_{14.07}, API_{14.07}) = \frac{1/n}{1 - U_{TP} - U_{API} + C(U_{TP}, U_{API})}$$

with  $U_X = F(x_{14.07})$  and C the copula

## **CDF-t correction**

- We apply the same statistical treatment to CMIP-6 Historic data (1950-2021) and CMIP-6 Projection data (2022-2100)
- For the moment, we have considered only the IPSL model, low resolution (ssp585)

CDF-t	Historic	Projection
Model (CMIP-6)	$F_{CMIPHist}$	F <sub>CMIPProj</sub> T
Reference (ERA5)	F <sub>ERA</sub> *	F <sub>Corrected</sub>

$$F_{Corrected}(x) = F_{ERA}(F^{-1}_{CMIPHist}\left(F_{CMIPProj}(x)\right))$$

 We get the corrected CDF, and then we perform a quantile-quantile correction between the corrected CDF and the projection data

## **Return periods results**

#### Return periods of the 14th July 2021 (ERA)



## **Return periods results**





# May/June French flooding

 Spatial daily precipitation means over the Seine and the Loire watersheds

• API :  $API_j = \sum_{i=1}^{i=N} k^{i-1} * TP_{j-i}$ with k=0.9 and N=20

Same methodology (Data selection, GPD model, copula ...)



### **Data selection**

API Seine for ERA, and data selected (red) Bivariate data selection API Seine (mm/day) 05 05 05 05 API Seine 6 Date (day) API Loire

#### **Quantile plots of GPD adjustment**

**QQplot Seine (ERA)** х XXXXXXXXXXX theoretical quantiles = -0,164 (0,116)

empirical quantiles



## Copula model



Data sets	Copula	X	$\overline{\chi}$
ERA	Survival Clayton	0,43	1
Historic	Survival Clayton	0,295	1
Projection	Joe	0,425	1
Projection corrected	Student	0,441	1

## **Return periods results**

#### Return Periods of May 2016 event (ERA)



## **Return periods results**

#### Return Periods of May 2016 event (comparison)





#### Next months :

- Multivariate bias correction
- Scale up framework to include more CMIP-6 simulations
- Paper

#### Next years :

• Apply treatment to convective cells