

# Estimating the impact of the COVID-19 pandemic on breast cancer: an application to life insurance

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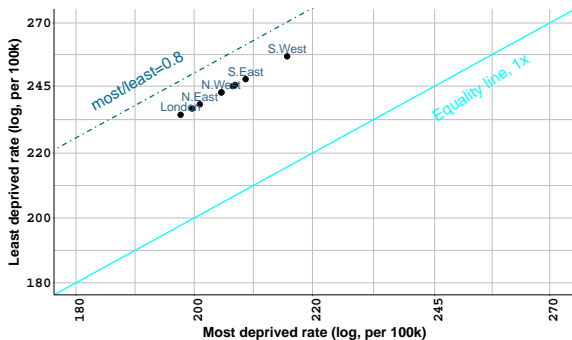
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  - Numerical applications
  - Summary

# Motivation: why breast cancer?

Breast cancer (BC) is

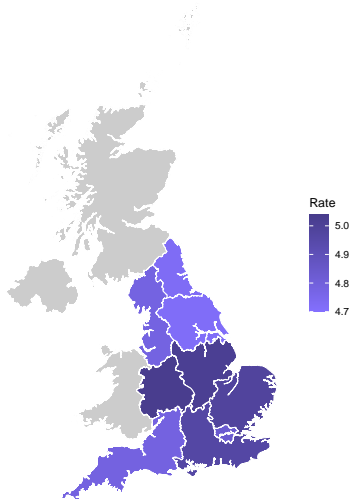
- **the most common** cancer diagnosed in women
- **one of the leading causes** of death for women
- one of the most **common** conditions amongst **critical illness insurance (CII) claims**, e.g. 44% of female CII claims in 2014 in the UK
- one of the cancer types where a **national cancer screening programme** is available

# Most v. least deprived by region: BC incidence in England - 2017



- Not a life-style cancer
- Rates for least deprived higher (higher screening?)
- Less regional variation as compared to, e.g., lung cancer

# Regional variation: BC mortality in England - 2019



✓ Rate is per 10K  
✓ Deprivation is  
not significant

# What insights we gain from BC data

- **Socio-economic differences** are **less relevant** as compared to, e.g., lung cancer incidence/mortality
- **Not** (easily) controllable or preventable risk factors
- **Regional inequality** exists but **relatively low**
  - High BC screening awareness
  - National BC screening programme for ages 47–73
- The availability of BC screening is crucial for early diagnosis, as BC can be curable

# Part 1: The impact of COVID-19 on breast cancer

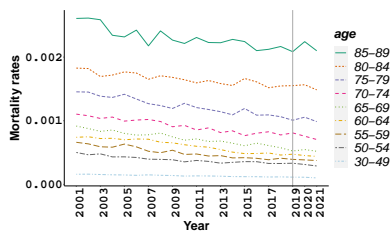
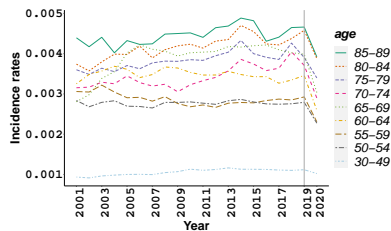
Investigate BC rates in the presence of:

- major disruptions to health services,

particularly caused by a catastrophic event, e.g. the COVID-19,

preventing or delaying the diagnosis of BC

# BC incidence and mortality in England: COVID years

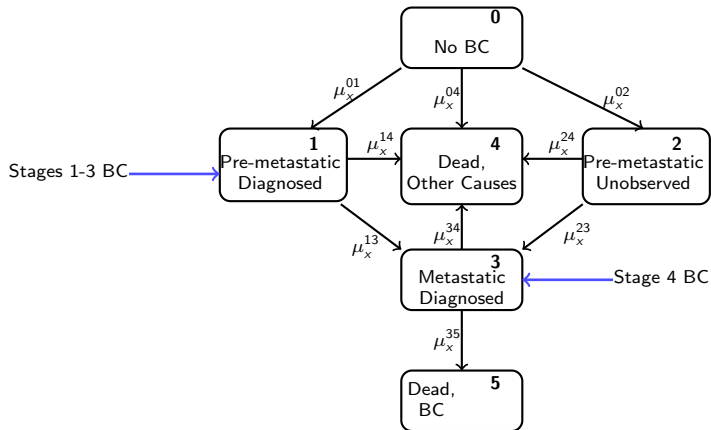


Incidence (left) v. Mortality (right)

- A significant decline in BC incidence, as low as 25% at ages 60–64, in 2020 as compared to the same period in 2019
- An increase in BC mortality from ages 65+, as high as 7%, in 2020 as compared to the same period in 2019

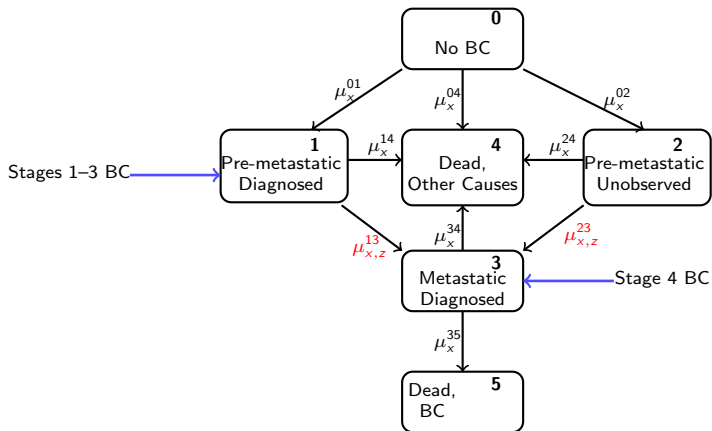


# Multi-state model for BC transitions: Markov model



- 'Dead from BC' is only accessible from 'Metastatic Diagnosed'
- Onset of BC remains unchanged  $\Rightarrow \mu_x^{01} + \mu_x^{02} = \mu_x^*$
- Treatment is available in 'Pre-metastatic Diagnosed'  
NOT in 'Pre-metastatic Unobserved'  $\Rightarrow \mu_x^{13} < \mu_x^{23}$

# Multi-state model for BC transitions: semi-Markov model



- Duration dependence in 'Pre-metastatic Diagnosed' and 'Pre-metastatic Unobserved'
- No treatment in 'Pre-metastatic Unobserved'  $\Rightarrow \mu_{x,z}^{13} < \mu_{x,z}^{23}$

# Modified Kolmogorov equations: semi-Markov model

$$\begin{aligned} \frac{d}{dt} {}_t p_x^{00} &= - {}_t p_x^{00} \left( \mu_{x+t}^{01} + \mu_{x+t}^{02} + \mu_{x+t}^{04} \right) \\ \frac{d}{dt} {}_t p_x^{01} &= {}_t p_x^{00} \mu_{x+t}^{01} - {}_t p_x^{01} \mu_{x+t}^{14} - \int_{u=0}^t {}_u p_x^{00} \mu_{x+u}^{01} {}_{t-u} p_{[x+u]}^{11} \mu_{[x+u]+t-u}^{13} du \\ \frac{d}{dt} {}_t p_x^{02} &= {}_t p_x^{00} \mu_{x+t}^{02} - {}_t p_x^{02} \mu_{x+t}^{24} - \int_{u=0}^t {}_u p_x^{00} \mu_{x+u}^{02} {}_{t-u} p_{[x+u]}^{22} \mu_{[x+u]+t-u}^{23} du \\ \frac{d}{dt} {}_t p_x^{03} &= \int_{u=0}^t {}_u p_x^{00} \mu_{x+u}^{01} {}_{t-u} p_{[x+u]}^{11} \mu_{[x+u]+t-u}^{13} du + \\ &\quad \int_{u=0}^t {}_u p_x^{00} \mu_{x+u}^{02} {}_{t-u} p_{[x+u]}^{22} \mu_{[x+u]+t-u}^{23} du - {}_t p_x^{03} \left( \mu_{x+t}^{34} + \mu_{x+t}^{35} \right) \\ \frac{d}{dt} {}_t p_x^{04} &= {}_t p_x^{00} \mu_{x+t}^{04} + {}_t p_x^{01} \mu_{x+t}^{14} + {}_t p_x^{02} \mu_{x+t}^{24} + {}_t p_x^{03} \mu_{x+t}^{34} \\ \frac{d}{dt} {}_t p_x^{05} &= {}_t p_x^{03} \mu_{x+t}^{35} \end{aligned}$$

- $\mu_{x,u}^{13} = \mu_{[x]+u}^{13}$  and  $\mu_{x,u}^{23} = \mu_{[x]+u}^{23}$  with select attained age  $[x]$  and duration  $u$
- Differential equations involve integration over duration  $u$

# A convenient parametrisation of the model

From

$$\mu_x^{01} + \mu_x^{02} = \mu_x^*$$

we can write

$$\begin{aligned}\mu_x^{01} &= \alpha \mu_x^* \\ \mu_x^{02} &= (1 - \alpha) \mu_x^*, \quad 0 < \alpha < 1\end{aligned}$$

$\alpha$  : level of BC diagnoses

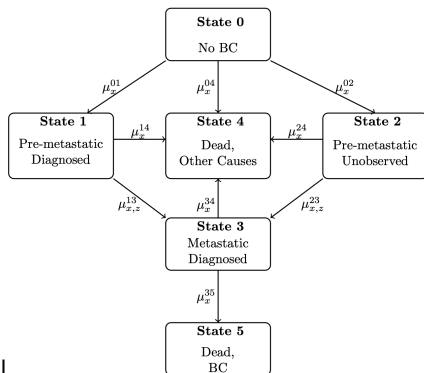
Also we assume

$$\mu_{x,z}^{13} = \beta \mu_{x,z}^{23}, \quad \beta < 1$$

$\beta$  : availability of BC treatment

Transitions to death due to other causes from all 'live' states are equal to  $\mu_x^{04}$

$$\mu_x^{14} = \mu_x^{24} = \mu_x^{34} = \mu_x^{04}$$

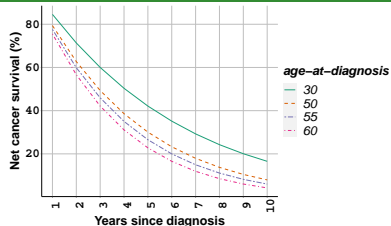
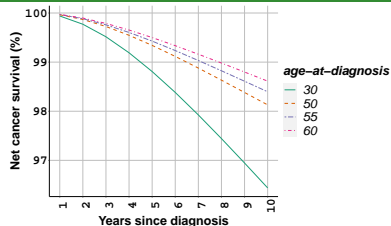


## BC model: pre-Covid rates

Age	$\mu_x^{01}$	$\mu_x^{04}$	$\mu_x^{35}$
30-49	0.00086	0.00084	0.16739
50-54	0.00224	0.00228	0.24005
55-59	0.00233	0.00363	0.24005
60-64	0.00282	0.00588	0.28060
65-69	0.00318	0.00952	0.28060
70-74	0.00280	0.01643	0.36002
75-79	0.00311	0.02987	0.40000
80-84	0.00338	0.05496	0.49711
85-89	0.00362	0.10112	0.50000

- $\mu_x^{01}$  : ONS/NHS Digital data, 81% of new BC registrations, England, 2001-2019
- $\mu_x^{04}$  : ONS data, deaths from other causes, England, 2001-2019
- $\mu_{x,z}^{13}$  : Average metastasis rates per 1000 person-years;  
 $\mu_x^{13} = 0.01954$  in the Markov model  
(Colzani et al., 2014)
- $\mu_x^{35}$  : BC deaths by age within 12 months after Stage 4 BC diagnosis  
(Zhao et al., 2020)

# BC net survival, semi-Markov model: pre-Covid rates



Pre-metastatic BC (left) v. Metastatic BC (right)

- Baseline scenarios are carried out for women when  $\alpha = 0.6$  and  $\beta = \frac{1}{7}$
- Net Survival: **ONLY** consider 'Dead, BC' as cause of death **AFTER** BC diagnosis
- An **unusual age pattern** in pre-metastatic BC net survival
- **Lower** metastatic BC net survival at older ages

For a woman aged  $x$ , diagnosed with pre-metastatic BC, BC survival in  $t$  years:

$$\frac{1 - {}_t p_x^{14} - {}_t p_x^{15}}{1 - {}_t p_x^{14}}$$

# BC model - COVID scenario

**In order to** quantify the impact of COVID-19 on BC mortality at older ages, we have

- Excess deaths from other causes,  
i.e. increase in  $\mu_x^{04}$
- Decline in BC diagnosis,  
i.e. slowdown in  $\mu_x^{01}$  and increase in  $\mu_x^{02}$

Pandemic period	$\mu_x^{01} / \mu_x^{02}$	$\mu_x^{04}$	
	$\alpha$	65–84	85–89
April–Nov. 2020	0.8	1.13	1.12
Dec. 2020–Nov. 2021	1	1.13	1.12
Dec. 2021–Dec. 2022	1	1.10	1.09
Jan.–Dec. 2023	1	1.07	1.06
Jan.–Dec. 2024	1	1.04	1.03

# Short-term implications up to 5 years

Occupancy Probabilities (%)											
From State 0											
Age	${}_5p_x^{00}$		${}_5p_x^{01}$		${}_5p_x^{02}$		${}_5p_x^{03}$		${}_5p_x^{04}$		${}_5p_x^{05}$
	M	M	S-M	M	S-M	M	S-M	M	M	S-M	
Pre-pandemic calibration											
65-69	93.09	1.50	1.47	0.76	0.68	0.24	0.31	4.29	0.13	0.16	
70-74	90.49	1.25	1.22	0.63	0.57	0.18	0.23	7.32	0.13	0.16	
75-79	85.07	1.33	1.31	0.67	0.61	0.18	0.24	12.59	0.15	0.19	
80-84	75.07	1.29	1.26	0.65	0.59	0.15	0.20	22.66	0.17	0.21	
85-89	59.71	1.09	1.07	0.55	0.50	0.13	0.17	38.36	0.16	0.19	
Pandemic scenario											
65-69	92.73	1.45	1.42	0.78	0.70	0.24	0.32	4.66	0.14	0.17	
70-74	89.90	1.20	1.18	0.65	0.58	0.18	0.24	7.93	0.14	0.17	
75-79	84.09	1.28	1.25	0.69	0.62	0.18	0.24	13.60	0.16	0.20	
80-84	73.42	1.22	1.20	0.66	0.59	0.16	0.21	24.36	0.18	0.22	
85-89	57.53	1.02	1.00	0.55	0.49	0.13	0.17	40.61	0.16	0.20	

- Semi-Markov (S-M) Model v. Markov (M) Model
- 3-6% decline in age-specific,  ${}_5p_x^{01}$ , 'Pre-metastatic Diagnosed'
- 3-5% increase in,  ${}_5p_x^{03}$ , 'Metastatic Diagnosed' (Vulnerability? Higher deaths from BC and other causes?)



# Changes in BC pre- v. post-pandemic

Age	Excess deaths				YLL			
	Dead (Other)		Dead (BC)		Dead (Other)		Dead (BC)	
	State 4		State 5		State 4		State 5	
	M	S-M	M	S-M	M	S-M	M	S-M
65-69	363	363	8	10	7000	7010	152	193
70-74	607	607	7	9	9298	9293	113	138
75-79	1011	1012	8	10	11762	11770	92	116
80-84	1699	1699	7	9	14342	14340	63	76
85-89	2253	2253	5	6	13158	13158	29	35

- 100,000 women in each age group, in 'No BC' at time zero, taken as January 1, 2020
- 3-6% increase in 'Dead from BC' in the semi-Markov (S-M) model;  
5-8% increase in the Markov (M) model;  
5-8% increase in 'Dead from Other Causes' for women, with 'No BC' at time zero, across different ages over 5 years

Years of life expectancy lost (YLL) from a given cause is:

$$YLL_{x,t}^{\text{cause}} = D_{x,t}^{\text{cause}} e_x$$

where  $D_{x,t}^{\text{cause}}$  is age- and type-specific additional deaths; and

$e_x$  is defined using standard life tables

# Summary (1)

- More equality in BC as compared to life-style cancers
- A valuable model relating to delays in the provision of BC diagnostic and treatment services
  - also relevant to meet the needs of women with medical history of BC
- As compared to the pre-pandemic scenario
  - 3–6% increase in deaths from BC and 5–8% from other causes between ages 65–89
  - Less than a 1% change in the probability of death for women with pre-metastatic BC ( ${}_5p_x^{15}$ )
  - A relatively significant change in the probability of death for women with metastatic BC ( ${}_5p_x^{35}$ ) as compared to women with pre-metastatic BC
- Measuring parameter and model uncertainty?

## Part 2: An application to life insurance products

A **considerable progress** in understanding BC due to

- medical research and data analysis

Better **options available** for people previously considered high-risk, e.g. **women with breast cancer history**

Examine existing models to see if they could lead to

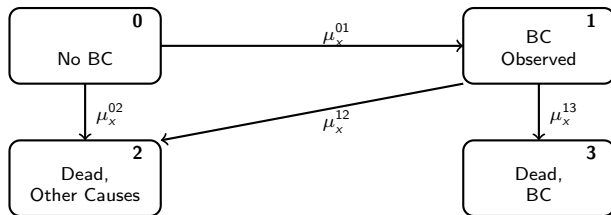
- fairly priced, more inclusive coverage options

# Critical illness and life insurance products

We consider

- single benefit in an insurance contract:  
a specialised CII  
OR  
a specialised life insurance (LI)
- benefit to be payable at the time of
  - 1 BC diagnosis or death from other causes in the CII contract
  - 2 death from any causes in the LI contract; and
- the LI contract can be purchased  
with pre-metastatic BC

# An industry-based Markov model



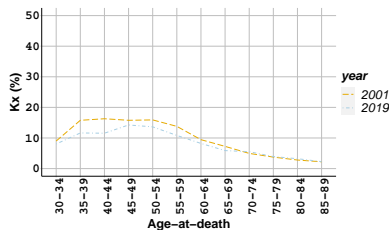
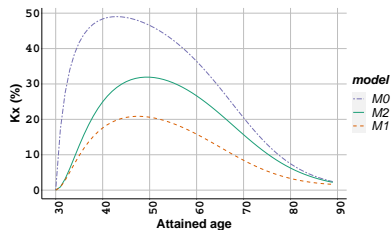
- A more compact version of the semi-Markov model
- Applied to CII by the insurance industry  
(Reynolds and Faye, 2016; Baione and Levantesi, 2018)
- **ONLY** account for observed BC cases
- Do not differentiate between different stages of BC

# All models: calibration

Age	$\mu_x^{01}$ in M0	$\mu_x^{01}$ in M1&M2	$\mu_x^{02}$ in M0 $\mu_x^{04}$ in M1&M2	$\mu_x^{13}$ in M0 $\mu_x^{35}$ in M1&M2
30–49	0.00106	0.00086	0.00084	0.16739
50–54	0.00277	0.00224	0.00228	0.24005
55–59	0.00287	0.00233	0.00363	0.24005
60–64	0.00349	0.00282	0.00588	0.28060
65–69	0.00393	0.00318	0.00952	0.28060
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80–84	0.00417	0.00338	0.05496	0.49711
85–89	0.00447	0.00362	0.10112	0.50000

- Industry-based (M0) Model v. Semi-Markov (M1) Model v. Markov (M2) Model
- $\mu_x^{01}$  : ONS/NHS Digital data, 81% of new BC registrations in M1&M2, England, 2001–2019
- $\mu_x^{02}$  or  $\mu_x^{04}$  : ONS data, deaths from other causes, England, 2001–2019
- $\mu_x^{13}$  or  $\mu_x^{35}$  : BC deaths by age within 12 months after Stage 4 BC diagnosis (Zhao et al., 2020)

# An industry-based approach: $k_x$ method



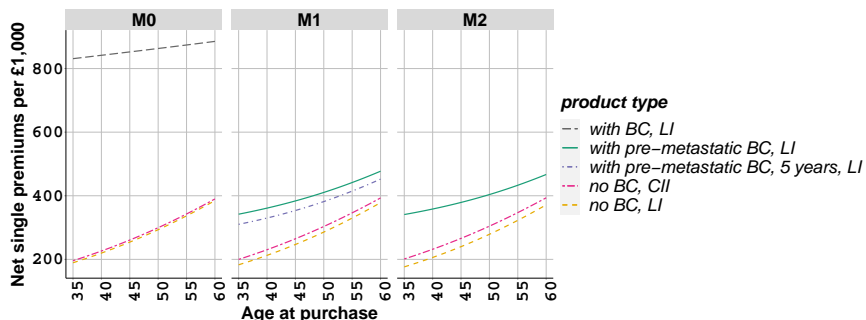
Implied  $k_x$  values (left) v. Observed  $k_x$  values (right)

- Industry-based (M0) Model v. Semi-Markov (M1) Model v. Markov (M2) Model
- Difficulty in calibrating models, in the *absence of good quality cause of deaths data*, especially relevant in CII context
- $k_x$  method is to **indirectly** define **deaths from other causes**, accepting the proportion of CI causes to be  $k_x\%$  of all deaths
- Significantly higher estimates under M0 (choice of  $\mu_x^{13}$  ?)

The proportion of BC deaths,  $k_x$  at attained age  $x$ , for instance, implied by M1 and M2

$$\hat{k}_x = \frac{{}_x p_0^{03} \mu_x^{35}}{{}_x p_0^{00} \mu_x^{04} + {}_x p_0^{01} \mu_x^{14} + {}_x p_0^{02} \mu_x^{24} + {}_x p_0^{03} \mu_x^{34} + {}_x p_0^{03} \mu_x^{35}}$$

# Net single premiums: whole life insurance



Whole life insurance contracts for  $i = 4\%$

- Industry-based (M0) Model v. Semi-Markov (M1) Model v. Markov (M2) Model
- Premiums, no BC, CII (lowest under M0) > Premiums, no BC, LI
- Premiums, diagnosed with pre-metastatic BC at the time of purchase, LI > Premiums, no BC, LI
- Premiums, diagnosed with pre-metastatic BC at the time of purchase, LI > Premiums, diagnosed with pre-metastatic BC 5 years before purchase, LI (Impact of duration or time spent with pre-metastatic BC? Vulnerability?)



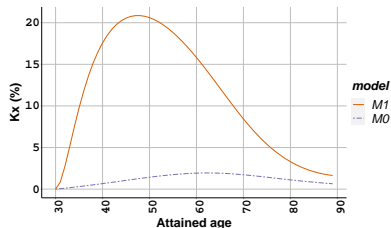
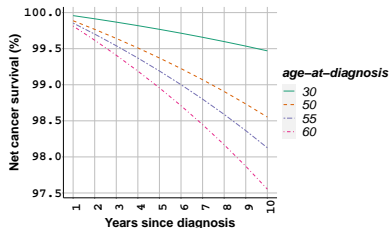
# What insights we gain from different models

- **Lower CII premiums** under the industry-based model, **M0**, due to
  - number of departures from 'No BC'
  - definition of rates of transition  $\mu_x^{01}$
  - absence of **unobserved BC cases**
- **Duration dependence** in the semi-Markov model, **M1**, enables
  - a **more** flexible and **inclusive** pricing methodology
  - results aligned with medical literature
- The **risk of death from BC under M0** is considered to be high, linked to the risk of dying from metastatic BC
  - leading to very high LI prices for a woman with BC
  - suggesting **sensitivity** to this assumption

# Sensitivity analysis

- Sensitivity analysis is carried out, all else equal, with
  - $\alpha = 0.4$  and  $\alpha = 0.8$  (lower v. higher BC diagnoses)
  - $\beta = \frac{1}{5}$  and  $\beta = \frac{1}{10}$  (worse v. better BC treatment)
  - $\mu_x^{35}$  is 20% lower and higher than the pre-pandemic level (lower v. higher BC deaths)
  - $i = 1-4\%$  (lower v. higher interest rates)
- **Consistent results** in relation to relative changes in net single premiums under different parametrisation

# Impact of definition of BC deaths: M0



BC survival under M0 (left) v. Implied  $k_x$  values (right)

- Industry-based (M0) Model v. Semi-Markov (M1) Model
- Baseline scenarios are carried out for women under M1 when  $\alpha = 0.6$  and  $\beta = \frac{1}{7}$
- The risk of death from BC under M0 is assumed to be similar to a woman with Stage 1 BC at the time of diagnosis
  - as opposed to be choosing this to be linked to Stage 4 BC
  - pointing sensitivity of M0
- The model is **NOT** capturing the age pattern in BC net survival as expected
- Very sensitive implied  $k_x$  values under M0

## Summary (2)

- New medical technologies improve cancer survival
- Flexible models are relevant to medical underwriting of related insurance contracts
- Less than 1% change in net single premiums when key transition rates are defined including COVID years
- Duration dependence matters in actuarial applications
- Smaller differences across premiums under different models with an increasing age and a longer time to maturity
- Accounting for time trend in cancer incidence, type-specific mortality, and the risk of developing metastatic BC?

## More details in:

- 1 Arık, A., Cairns, A., Dodd, E., Macdonald, A.S., Shao, A., Streftaris, G. Insurance pricing for breast cancer under different multiple state models, working paper.
- 2 Arık, A., Cairns, A., Dodd, E., Macdonald, A.S., Streftaris, G. The effect of the COVID-19 health disruptions on breast cancer mortality for older women: A semi-Markov modelling approach, <https://arxiv.org/abs/2303.16573>.
- 3 Arık, A., Cairns, A., Dodd, E., Macdonald, A.S., Streftaris, G. Estimating the impact of the COVID-19 pandemic on breast cancer deaths among older women, Living to 100 Research Symposium, 16 February 2023, conference monograph.
- 4 Arık, A., Dodd, E., Cairns, A., Streftaris, G. Socioeconomic disparities in cancer incidence and mortality in England and the impact of age-at-diagnosis on cancer mortality, PLOS ONE, 2021.
- 5 Arık, A., Dodd, E., Streftaris, G. Cancer morbidity trends and regional differences in England - a Bayesian Analysis, PLOS ONE, 2020.

# Thank You!

## Questions?

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