Scope and limits of artificial intelligence

Arthur Charpentier

SCOR Foundation - 2024

harpentier, 2024 SCOR

Bio (short)

Arthur Charpentier Professor at Université du Québec à Montréal, 🏶

- > Denuit and Charpentier (2004, 2005) Mathématiques de l'Assurance Non-Vie,
- > Charpentier (2014) Computational Actuarial Science with R,
- > Bénéplanc et al. (2022) Manuel d'Assurance,
- > Charpentier (2024) Insurance: Biases, Discrimination and Fairness.



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François Hu Postdoctoral fellow, Université de Montréal

Philipp Ratz PhD Student, Université du Québec à Montréal

Agathe Fernandes-Machado PhD Student, Université du Québec à Montréal

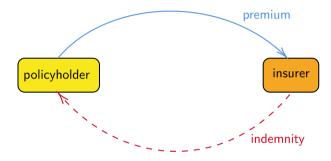
Olivier Côté PhD Student, Université Laval, Québec



Also interns Ana Patrón Piñerez and Suzie Grondin, 🏶

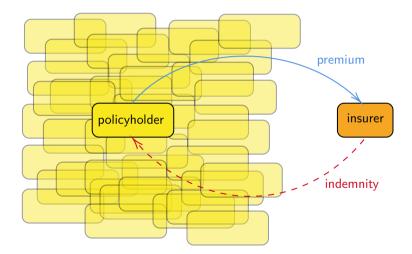
Insurance (and "Actuarial Fairness")

> Insurance is a risk transfer (from a policyholder to an insurance company)



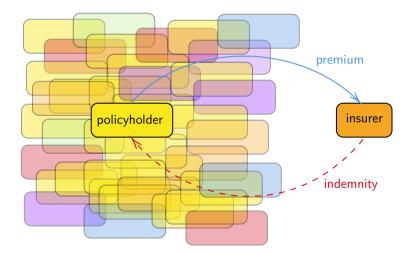
Insurance (and "Actuarial Fairness")

> "Insurance is the contribution of the many to the misfortune of the few"



Insurance (and "Actuarial Fairness")

> "Insurance is the contribution of the many to the misfortune of the few"

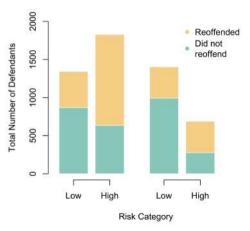


Motivation (1. Propublica, Actuarial Justice)

- Concept of "actuarial justice" as coined in Feeley and Simon (1994)
- Correctional Offender Management Profiling for Alternative Sanctions (COMPAS), Perry (2013)

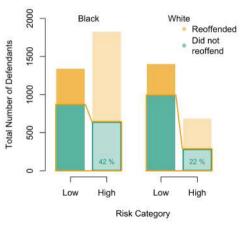


 https://github.com/propublica/compas-analysis
 Angwin et al. (2016) Machine Bias Dressel and Farid (2018)



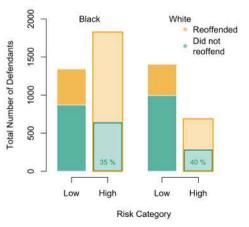
Motivation (1. Propublica, Actuarial Justice)

- > From Feller et al. (2016),
 - for White people, among those who did not re-offend, 22% were wrongly classified,
 - for Black people, among those who did not re-offend, 42% were wrongly classified,
 - problem, since $42\% \gg 22\%$



Motivation (1. Propublica, Actuarial Justice)

- > From Dieterich et al. (2016),
 - for White people, among those who where classified as high risk, 40% did not re-offend,
 - for Black people, among those who where classified as high risk, 35% did not re-offend,
 - ▶ no problem, since $40\% \approx 35\%$



> EU Directive (2004/113/EC), 2004 version

- Article 5 (Actuarial factors) -

1. Member States shall ensure that in all new contracts concluded after 21 December 2007 at the latest, the use of sex as a factor in the calculation of premiums and benefits for the purposes of insurance and related financial services shall not result in differences in individuals' premiums and benefits.

2. Notwithstanding paragraph 1, Member States may decide before 21 December 2007 to permit proportionate differences in individuals' premiums and benefits where the use of sex is a determining factor in the assessment of risk based on relevant and accurate actuarial and statistical data. The Member States concerned shall inform the Commission and ensure that accurate data relevant to the use of sex as a determining actuarial factor are compiled, published and regularly updated.

Au Québec, Charte des droits et libertés de la personne (C-12)

– Article 20.1 –

Dans un contrat d'assurance ou de rente, un régime d'avantages sociaux, de retraite, de rentes ou d'assurance ou un régime universel de rentes ou d'assurance, une distinction, exclusion ou préférence fondée sur l'âge, le sexe ou l'état civil est réputée non discriminatoire lorsque son utilisation est légitime et que le motif qui la fonde constitue un facteur de détermination de risque, basé sur des données actuarielles.



> September 27, 2023, the Colorado Division of Insurance exposed a new proposed regulation entitled Concerning Quantitative Testing of External Consumer Data and Information Sources, Algorithms, and Predictive Models Used for Life Insurance Underwriting for Unfairly Discriminatory Outcomes

– Section 5 (Estimating Race and Ethnicity) –

Insurers shall estimate the race or ethnicity of all proposed insureds that have applied for coverage on or after the insurer's initial adoption of the use of ECDIS, or algorithms and predictive models that use ECDIS, including a third party acting on behalf of the insurer that used ECDIS, or algorithms and predictive models that used ECDIS, in the underwriting decision-making process, by utilizing: BIFSG and the insureds' or proposed insureds' name and geolocation (...)

- Bayesian Improved First Name Surname Geocoding, or "BIFSG"
- > External Consumer Data and Information Source, or "ECDIS"



EU Directive (2010/41/EU), 2010 version (on the application of the principle of equal treatment between men and women)

- Article 3 (Definition) -

(a) 'direct discrimination': where one person is treated less favourably on grounds of sex than another is, has been or would be, treated in a comparable situation;

(b) 'indirect discrimination': where an apparently neutral provision, criterion or practice would put persons of one sex at a particular disadvantage compared with persons of the other sex, unless that provision, criterion or practice is objectively justified by a legitimate aim, and the means of achieving that aim are appropriate and necessary;



In France, Loi n° 2008-496 du 27 mai 2008

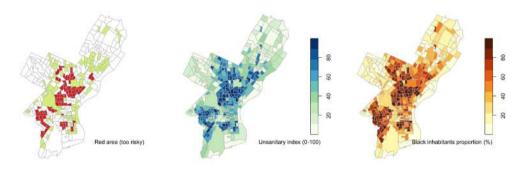
– Article 1 –

Constitue une discrimination indirecte une disposition, un critère ou une pratique neutre en apparence, mais susceptible d'entraîner, pour l'un des motifs mentionnés au premier alinéa, un désavantage particulier pour des personnes par rapport à d'autres personnes, à moins que cette disposition, ce critère ou cette pratique ne soit objectivement justifié par un but légitime et que les moyens pour réaliser ce but ne soient nécessaires et appropriés.

Extension of "Loi n° 72-546 du 1 juillet 1972", which removed the requirement for specific intent.



Motivation (3. Redlining)



(Fictitious maps, inspired by a Home Owners' Loan Corporation map from 1937)

- Federal Home Loan Bank Board (FHLBB) "residential security maps" (for real-estate investments), Crossney (2016) and Rhynhart (2020)
- Unsanitary index and proportion of Black inhabitants
- Discrimination as an "ill-posed problem"?

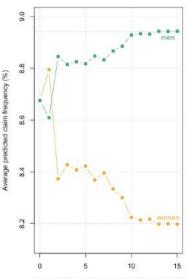
Motivation (4. Proxies)

> On a French motor dataset, average claim frequencies are 8.94% (men) 8.20% (women).

Consider some logistic regression to estimate annual claim frequency, on k explanatory variables excluding gender.

	men	women
k = 0	8.68%	8.68%
k = 2	8.85%	8.37%
k = 8	8.87%	8.33%
k = 15	8.94%	8.20%
empirical	8.94%	8.20%

> Models simply tend to reproduce what was observed in the data (see "is-ought" problem, in Hume (1739)).



Number of explanatory variables (without gender)

Discrimination and Insurance

"Machine learning won't give you anything like gender neutrality 'for free' that you didn't explicitely ask for," Kearns and Roth (2019)

"What is unique about insurance is that even statistical discrimination which by definition is absent of any malicious intentions, poses significant moral and legal challenges. Why? Because on the one hand, policy makers would like insurers to treat their insureds equally, without discriminating based on race, gender, age, or other characteristics, even if it makes statistical sense to discriminate (...) On the other hand, at the core of insurance business lies discrimination between risky and non-risky insureds. But riskiness often statistically correlates with the same characteristics policy makers would like to prohibit insurers from taking into account." Avraham (2017)

"Technology is neither good nor bad; nor is it neutral," Kranzberg (1986)

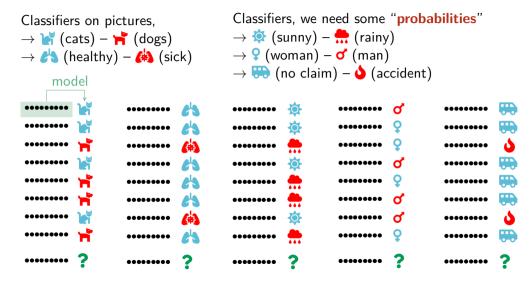
Agenda

interpretability

	sufficiency		separation	independence	
calil	bration				

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Classifiers (or why actuarial science \neq computer science)



Fairness for Classifiers

Following Barocas et al. (2017), standard definitions are

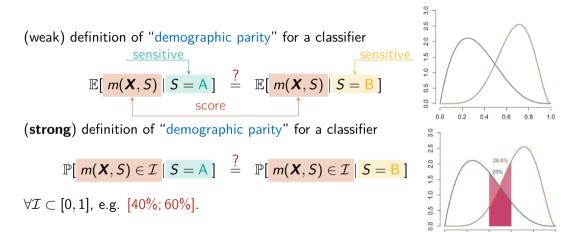
$$\mathsf{score} \in [0,1] \subset \mathbb{R}$$

A model *m* satisfies the **independence property** if $m(X, S) \perp S$, with respect to the distribution \mathbb{P} of the triplet $(X, S, Y) \leftarrow \text{demographic parity}$

A model satisfies the **separation property** if $m(X, S) \perp S \mid Y$, with respect to the distribution \mathbb{P} of the triplet $(X, S, Y) \leftarrow$ equalized odds

A model satisfies the sufficiency property if $Y \perp S \mid m(X, S)$, with respect to the distribution \mathbb{P} of the triplet $(X, S, Y) \leftarrow \text{calibration}$

Fairness for Classifiers



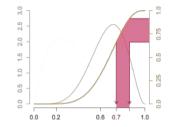
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Fairness for Classifiers using Optimal Transport

$$F_A(u) = \mathbb{P}[m(\boldsymbol{X}, S) \leq u \mid S = A]$$

$$F_{B}(u) = \mathbb{P}[m(\boldsymbol{X}, S) \leq u | S = B]$$

and F_B denote the cumulative distribution function of scores in group B Consider individuals in group A such that



$$m(X,S) \in [0.4;0.6] \mid S = A$$
 then ranks $(m(X,S)) \in [66.3\%;91.3\%] \mid S = A$

then, in group B

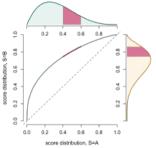
if ranks
$$(m(X, S)) \in [66.3\%; 91.3\%] | S = B$$
 then $m(X, S) \in [0.743; 0.861] | S = B$

Fairness for Classifiers using Optimal Transport

$$F_A(u) = \mathbb{P}[m(\boldsymbol{X}, S) \leq u \mid S = A]$$

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and F_B denote the cumulative distribution function of scores in group B Consider individuals in group A such that



$$m(\boldsymbol{X}, S) \in [0.4; 0.6] \mid S = A$$

then, in group B $(optimal transport mapping T^*)$
if ranks $(m(\boldsymbol{X}, S)) \in [66.3\%; 91.3\%] \mid S = B$ then $m(\boldsymbol{X}, S) \in [0.743; 0.861] \mid S = B$

Formalizing Optimal Transport

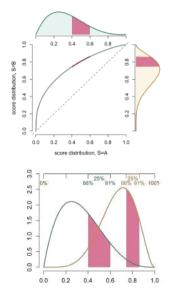
Consider the following $[0,1] \rightarrow [0,1]$ mapping

$$T^{\star}(x) = F_{B}^{-1} \circ F_{A}(x)$$

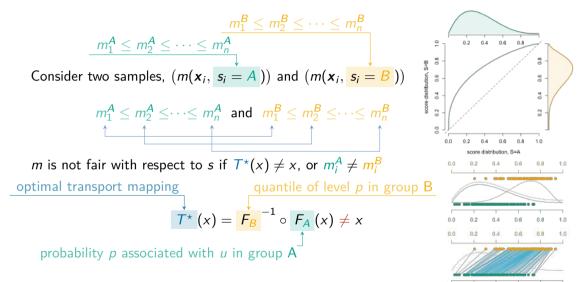
$$\mathcal{T}^{\star} = \operatorname*{argmin}_{\mathcal{T}:[0,1] \to [0,1]} \int_{0}^{1} \left(\frac{\mathcal{T}(x)}{\mathcal{T}(x)} - x \right)^{2} dF_{\mathcal{A}}(x)$$

i.e.
$$\underset{T:[0,1]\to[0,1]}{\operatorname{argmin}} \mathbb{E}\left[\left(\begin{array}{c} \mathcal{T}(X) \\ \mathcal{F}_A \end{array}\right)^2\right]$$
 where $X \sim \mathcal{F}_A$,

corresponding to Monge (1781) problem, revisited by Kantorovich (1942). (the minimum value is called **Wasserstein distance**)



Optimal Transport with a Finite Sample (another interpretation)



Mitigating Discrimination with Wasserstein Barycenters

Mitigation is about finding some *m*^{*} "in-between" (Demographic Parity)

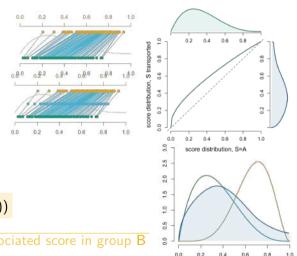
For individual *i*, why not

$$m_i^{\star} = \frac{1}{2}m_i^{\mathcal{A}} + \frac{1}{2}m_i^{\mathcal{B}}$$

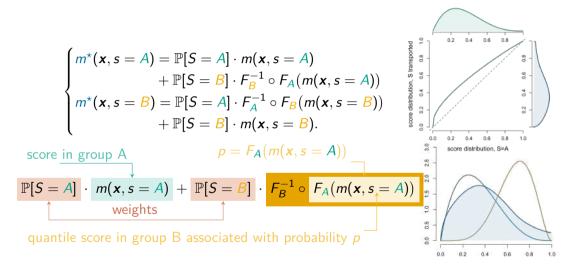
corresponding to

$$m^{\star}(x,A) = \frac{1}{2}m^{A}(x) + \frac{1}{2}T^{\star}(m^{A}(x))$$

$$\mathbb{P}[S=A] \xrightarrow{\mathbb{P}[S=B]} \xrightarrow{$$



Mitigating Discrimination with Wasserstein Barycenters



Mitigating Discrimination with Wasserstein Barycenters

$$\begin{cases} m^{\star}(x, s = A) = \mathbb{P}[S = A] \cdot m(x, s = A) \\ + \mathbb{P}[S = B] \cdot F_{B}^{-1} \circ F_{A}(m(x, s = A)) \\ m^{\star}(x, s = B) = \mathbb{P}[S = A] \cdot F_{A}^{-1} \circ F_{B}(m(x, s = B)) \\ + \mathbb{P}[S = B] \cdot m(x, s = B). \end{cases}$$

$$p = F_{B}(m(x, s = B))$$

$$p = F_{B}(m(x, s = B))$$

$$p = F_{B}(m(x, s = A)) + \mathbb{P}[S = B] \cdot m(x, s = B)$$

$$p = F_{B}(m(x, s = A)) + \mathbb{P}[S = B] \cdot m(x, s = B)$$

Back to the COMPAS Example

 $\begin{cases} S : \text{ race (binary), black & white} \\ Y : \text{ re-offense (binary), no & yes} \\ \widehat{Y} : \text{ classifier (risk category), low & high} \end{cases}$

(standard) demographic parity would be translated as

$$\mathbb{P}[\hat{Y} = \text{high}, S = \text{black}] = 58\% \stackrel{?}{=} \mathbb{P}[\hat{Y} = \text{high}, S = \text{white}] = 33\%,$$
predictions

Back to the COMPAS Example, from Discrimination to Calibration

 $\begin{cases} S : \text{ race (binary), black & white} \\ Y : \text{ re-offense (binary), no & yes} \\ \widehat{Y} : \text{ classifier (risk category), low & high} \end{cases}$

$$\mathbb{P}[\hat{Y} = \text{high}|Y = \text{no}, S = \text{black}] = 42\% \stackrel{?}{=} \mathbb{P}[\hat{Y} = \text{high}|Y = \text{no}, S = \text{white}] = 22\%,$$
false positive rate

$$\mathbb{P}[|Y = no|\hat{Y} = high|, |S = black|] = 35\% \stackrel{?}{=} \mathbb{P}[|Y = no|\hat{Y} = high|, |S = white|] = 40\%.$$
false discovery rate

From Discrimination to Calibration

$$\begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \text{sensitive} \\ \text{demographic parity} \end{array} \rightarrow \\ \mathbb{E}[m(\textbf{X},S) \mid \textbf{S} = \textbf{A}] \end{array} \stackrel{?}{=} \\ \mathbb{E}[m(\textbf{X},S) \mid \textbf{S} = \textbf{B}] \\ \hline \\ \begin{array}{c} \begin{array}{c} \begin{array}{c} \text{sensitive} \\ \text{sensitive} \end{array} \end{array} \stackrel{}{=} \\ \mathbb{E}[m(\textbf{X},S) \mid \textbf{Y} = \textbf{y}, \\ \textbf{S} = \textbf{A}] \end{array} \stackrel{?}{=} \\ \mathbb{E}[m(\textbf{X},S) \mid \textbf{Y} = \textbf{y}, \\ \textbf{S} = \textbf{B}], \\ \forall \textbf{y} \end{array} \end{array}$$

$$\begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \text{sensitive} \\ \text{sensitive} \end{array} \stackrel{}{=} \\ \mathbb{E}[m(\textbf{X},S) \mid \textbf{Y} = \textbf{y}, \\ \textbf{S} = \textbf{B}] \end{array} \stackrel{}{=} \\ \mathbb{E}[m(\textbf{X},S) \mid \textbf{Y} = \textbf{y}, \\ \textbf{S} = \textbf{B}], \\ \forall \textbf{y} \end{array}$$

$$\begin{array}{c} \begin{array}{c} \begin{array}{c} \text{sensitive} \\ \text{sensitive} \end{array} \stackrel{}{=} \\ \mathbb{E}[\textbf{Y} \mid m(\textbf{X},S) = u, \\ \textbf{S} = \textbf{B}] \end{array} \stackrel{}{=} \\ \mathbb{E}[\textbf{Y} \mid m(\textbf{X},S) = u, \\ \textbf{S} = \textbf{B}], \\ \forall u \end{array}$$

From Discrimination to Calibration (an Epistemological Detour)

$$\underbrace{\frac{1}{n}\sum_{i=1}^{n}\mathbf{1}(X_{i}\in\mathcal{A})}_{\text{(empirical) frequency}} \xrightarrow{\text{a.s.}} \underbrace{\mathbb{P}(\{X\in\mathcal{A}\})}_{\text{probability}} = \mathbb{P}[X\in\mathcal{A}], \text{ as } n\to\infty.$$

"When we speak of the 'probability of death', the exact meaning of this expression can be defined in the following way only. We must not think of an individual, but of a certain class as a whole, e.g., 'all insured men forty-one years old living in a given country and not engaged in certain dangerous occupations'. A probability of death is attached to the class of men or to another class that can be defined in a similar way. We can say nothing about the probability of death of an individual even if we know his condition of life and health in detail. The phrase 'probability of death', when it refers to a single person, has no meaning for us at all," von Mises (1928, 1939)

From Discrimination to Calibration (an Epistemological Detour)

This frequentist approach is unable to make sense of the probability of a "single singular event".

$$\underbrace{\sum_{i=1}^{n} Y_{i} \cdot \mathbf{1}(X_{i} \in \mathcal{A})}_{\substack{\sum_{i=1}^{n} \mathbf{1}(X_{i} \in \mathcal{A})}} \xrightarrow{a.s.} \underbrace{\mathbb{E}(Y|X \in \mathcal{A})}_{expected value}, \text{ as } n \to \infty.$$

Property $\mathbb{E}[Y \mid m(X, S) = u] = u, \forall u \in [0, 1]$ corresponds to "calibration".

"Out of all the times you said there was a 40 percent chance of rain, how often did rain actually occur? If, over the long run, it really did rain about 40 percent of the time, that means your forecasts were well calibrated," Silver (2012)

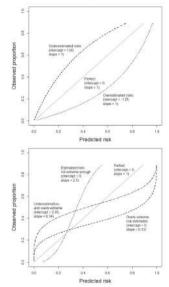
From Discrimination to Calibration (an Epistemological Detour)

As explained in Van Calster et al. (2019), "among patients with an estimated risk of 20%, we expect 20 in 100 to have or to develop the event,"

- If 40 out of 100 in this group are found to have the disease, the risk is underestimated
- If we observe that in this group, 10 out of 100 have the disease, we have overestimated the risk.

Most machine learning models can be poorly calibrated, Denuit et al. (2021), Machado et al. (2024).

(picture source: Van Calster et al. (2019))



From Discrimination to Calibration



female (0.984) male (0.016)



female (0.009) male (0.991)



female (0.983)

male (0.017)

female (0.014) male (0.986)



female (0.982) male (0.018)





female (0.960) male (0.040)



female (0.015) male (0.985)

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Individual Fairness

We have **counterfactual fairness** if "had the protected attributes (e.g., race) of the individual been different, other things being equal, the decision would have remained the same," Kusner et al. (2017)

"Ladder of causation" from Pearl IUDEA PEARL WINNER OF THE TURING AWARD. et al. (2009). Pearl and Mackenzie AND DANA MACKENZIE 5. COUNTERFACTUALS (2018)ACTIVITY, Income Representation THE CONTRACT The Contract Of Charles of Contract View Contract AGINING TRAMBTS. Was in the aspin is that they well not been had as 3. Counterfactuals BOOK OF (Imagining, "what if I had done...") 2. INITERA/ENITIONS ACTIVITY: Item Immune DOING WHY 2 Intervention > EXAMPLE: WIthin some will an hadde in provi-Wheel & its bettingentled (Doing. "what if I do...") 1 ASSOCIATION ACTIVITY: thread (Colorado CONTRACT EASTING 1. Association They are the plaudites related? THE NEW SCIENCE How totald turing X change are balled as T() SHAMP IS. When there a manuser of the dame a flower OF CAUSE AND FFFECT (Seeing, "what if I see...")

Fairness for Attributed Networks

Taking into account neighbors is more complicated Classical paradoxes on probabilities and averages, "on average your friends have more friends than you do."

Homophily is the tendency of individuals to form relations with others similar to them.

Neighborhood-peer expectation $\mathbb{E}_{\mathcal{G}, \boldsymbol{X}}$ is

$$\mathbb{E}_{\mathcal{G},\boldsymbol{X}}[h(i)] = \frac{1}{\sum_{j\in N_i} k(i,j)} \sum_{j\in N_i} h(j)k(i,j),$$

where $k(i,j) \propto \|\boldsymbol{x}_i - \boldsymbol{x}_j\|$.

Crash course in July 2024 on Collaborative insurance, unfairness and discrimination, 🏶

What About Interpretation ?

"Humans think in stories rather than facts, numbers or equations - and the simpler the story, the better," Harari (2018)

For Glenn (2000), insurer's risk selection process has two sides:
the one presented to regulators and policyholders (numbers, statistics and objectivity),

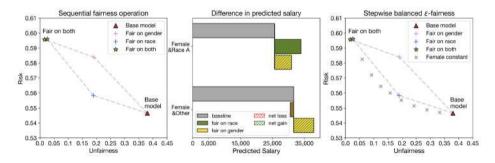
> the other presented to underwriters (stories, character and subjective judgment).

The rhetoric of insurance exclusion – numbers, objectivity and statistics – forms what Brian Glenn calls "the myth of the actuary," "a powerful rhetorical situation in which decisions appear to be based on objectively determined criteria when they are also largely based on subjective ones" or "the subjective nature of a seemingly objective process".

What About Interpretation ?

"The fact that the selection of risk factors is subjective and contingent upon narratives of risk and responsibility has in the past played a far larger role than whether or not someone with a wood stove is charged higher premiums."

Going further, "virtually every aspect of the insurance industry is predicated on stories first and then numbers," Glenn (2003)



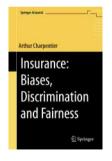
Mitigating Discrimination ? (brief conclusion)

If it is mandatory to mitigate, there are robust techniques that can guarantee fairness

Supreme Court Justice Harry Blackmun stated, in 1978, "In order to get beyond racism, we must first take account of race. There is no other way. And in order to treat some persons equally, we must treat them differently," Knowlton (1978), cited in Lippert-Rasmussen (2020)

In 2007, John G. Roberts of the U.S. Supreme Court submits "The way to stop discrimination on the basis of race is to stop discriminating on the basis of race," Sabbagh (2007) and Turner (2015)

To go further, Charpentier (2024) Insurance: Biases, Discrimination and Fairness.



Mitigating Discrimination ? (brief conclusion)



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